

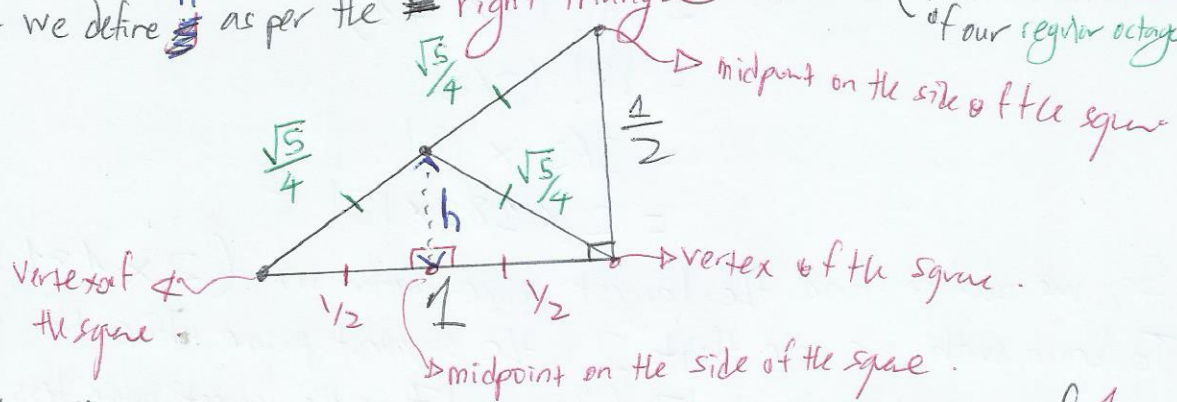
Muda

(B1) Note that the shaded region is a regular octagon (by symmetry).

We exploit the symmetry of the regular octagon in 2 ways:

Firstly define: r = radius of the excircle or the circumscribing circle of the regular octagon.

Next we define h as per the right triangle below (found at the corners of our regular octagon).



Note that our square which has an area of 1 also has a side of 1.

By applying Pythagoras theorem $(\frac{1}{2})^2 + 1^2 = (\frac{\sqrt{5}}{4} + \frac{\sqrt{5}}{4})^2$ to the larger right triangle, we obtain the value $\frac{\sqrt{5}}{4}$.

Now, by applying Pythagoras theorem on the smaller right triangle (with leg h), we obtain: $h^2 + (\frac{1}{2})^2 = (\frac{\sqrt{5}}{4})^2$ solve to get $h = \frac{1}{4}$

We also the diameter of the regular octagon which is both parallel and equal to the side (length = 1) of the square as follows:

Note that: $\frac{180^\circ}{4} = 45^\circ$

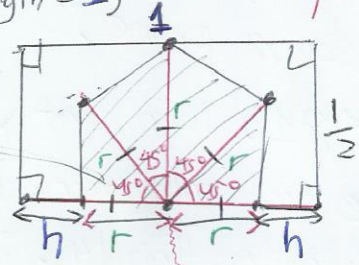
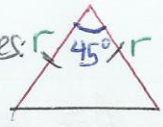


Diagram shows "half" the square. (not to scale). A rectangle is formed. [half of the regular octagon is inside]

use here! Comparing the top and bottom sides of this rectangle, (which are equal), we get: $h + r + r + h = 1 \rightarrow r = \frac{1}{2} - h \rightarrow r = \frac{1}{2} - \frac{1}{4} \rightarrow r = \frac{1}{4}$

Finally we note that our regular octagon is made up of 8 congruent isosceles triangles: r 45° r where Each of these has an Area, $A = \frac{1}{2} r^2 \sin 45^\circ$



$$A = \frac{1}{2} \times (\frac{1}{4})^2 \times (\frac{1}{\sqrt{2}})$$

$$\Rightarrow A = \frac{1}{32\sqrt{2}} \rightarrow \text{Area of regular octagon} = 8A = \frac{1}{4\sqrt{2}}$$

(Pg 14) Thus Answer = $\frac{1}{4\sqrt{2}}$