

OMK 2014 - Sulong (3 July 2019)

(B2) Lastly, referring back to (1)

$$\left(\text{Number of good subsets} \right) = 2 \times \left(\text{NO. of subsets of } \{1, 2, 3, \dots, 2011\} \text{ whose sum of its elements is divisible by 3} \right)$$

$$= 2 \times A_0$$

$$= 2 \times \left[\frac{2^{2011} + 2^{670}}{3} \right]$$

using 13

$$= \frac{2^{2012} + 2^{671}}{3}$$

$$= \frac{2^{671} (2^{1341} + 1)}{3}$$

So

$$\text{Answer: } \left(\frac{2^{2012} + 2^{671}}{3} \right) \text{ or } \left(\frac{2^{671} (2^{1341} + 1)}{3} \right)$$