

(B3) This solution is gonna be a little long. So I'll skip the explanation way and just present the solution directly.

For starters, we define intelligently some real number K_i based on a positive integer m_i as follows:

$$\text{Let } K_i = \frac{m_i \cdot 2^{m_i}}{(2^{m_i} - 1)}, \text{ where } m_i = i \text{ for all } i \geq 1 \text{ and } i \text{ is an arbitrary positive integer.}$$

(e.g. $m_1 = 1, m_2 = 2, m_3 = 3$... etc...)

In fact we can see that K_i 's are actually rational numbers.

Now, note an interesting property of the K_i 's.

* Property (1):

Each m_i would produce a unique K_i (because K_i increases as m_i increases across the positive integers), here's a proof:

We wish to prove that:

$$K_{i+1} > K_i$$

which is equivalent to all the implications below (can be ~~proved~~ implied backwards):

$$\frac{m_{i+1} \cdot 2^{m_{i+1}}}{(2^{m_{i+1}} - 1)} > \frac{m_i \cdot 2^{m_i}}{(2^{m_i} - 1)}$$

$$\frac{(z+1) \cdot 2^{z+1}}{(2^{z+1} - 1)} > \frac{z \cdot 2^z}{(2^z - 1)}$$

Thus its truth implied backwards):
note by definition:
 $m_{i+1} = i+1 = m_i + 1$
So, for simplicity
let $m_i = z$

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