

Sulong

B3 (continued from the earlier page).

We prove property ② as follows:

$$\text{By definition, } K_i = \frac{m_i \cdot 2^{m_i}}{(2^{m_i} - 1)}$$

For simplicity in writing our proof, temporarily let $K = K_i$ and $m = m_i$ so that our definitions may be written as:

$$K = \frac{m \cdot 2^m}{(2^m - 1)}$$

$$K(2^m - 1) = m \cdot 2^m$$

$$2^m \cdot K - K = m \cdot 2^m$$

$$2^m \cdot K = m \cdot 2^m + K$$

$$2^m \cdot K - m \cdot 2^m = K$$

$$2^m (K - m) = K$$

Or just,

$$2^m = \frac{K}{(K - m)}$$

Replacing back our $m_i = m$ and $K_i = K$ respectively into the above, we obtain our deduction (proved):

$$2^{m_i} = \frac{K_i}{(K_i - m_i)}$$

Property
QED - ②